

# Statistical Models for Forest Ecology



Prof. Albert Y. Kim  
Environmental Science & Policy Lunchbag  
Wednesday, September 30, 2020



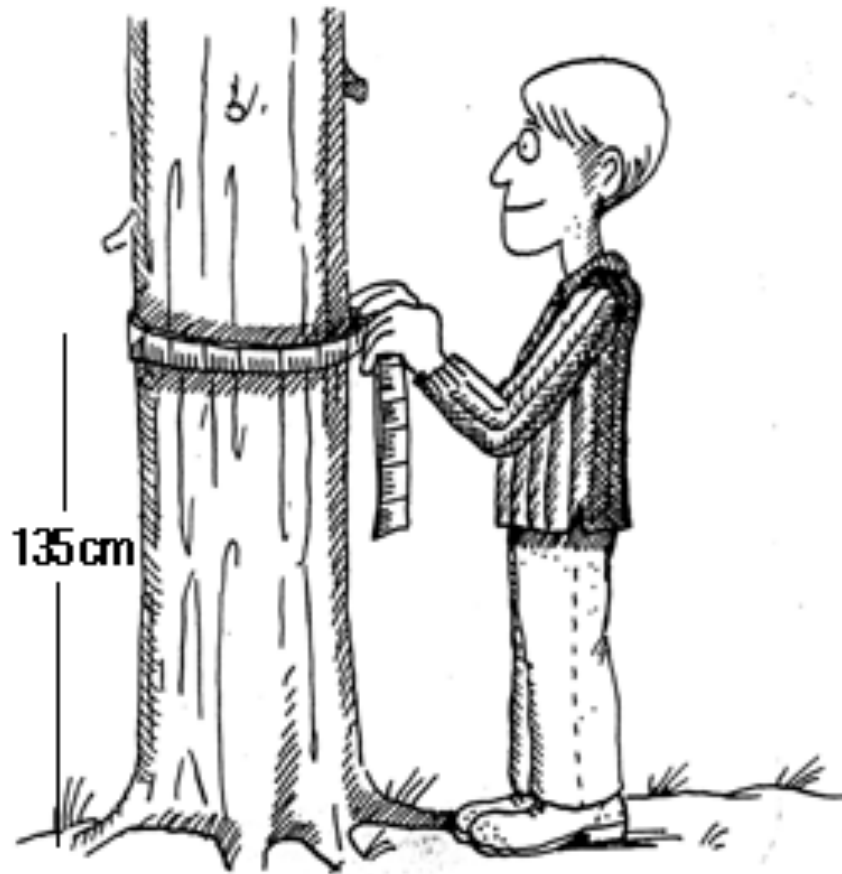
# Diameter at Breast Height (dbh)

After species & location, one of the most informative variables about a tree is dbh



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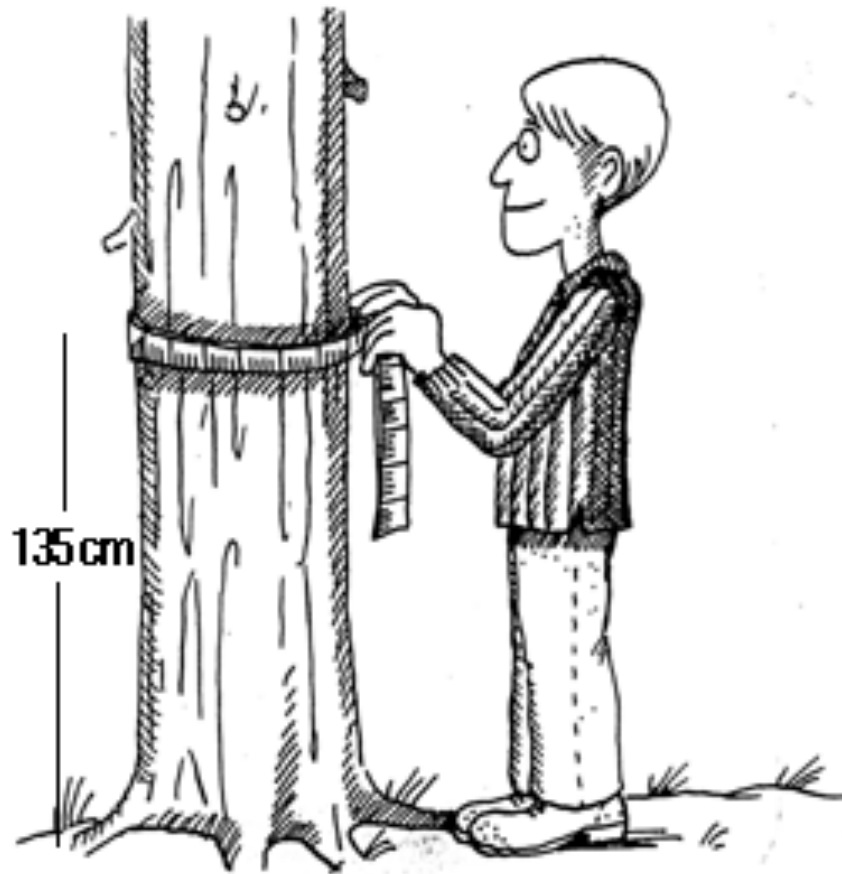
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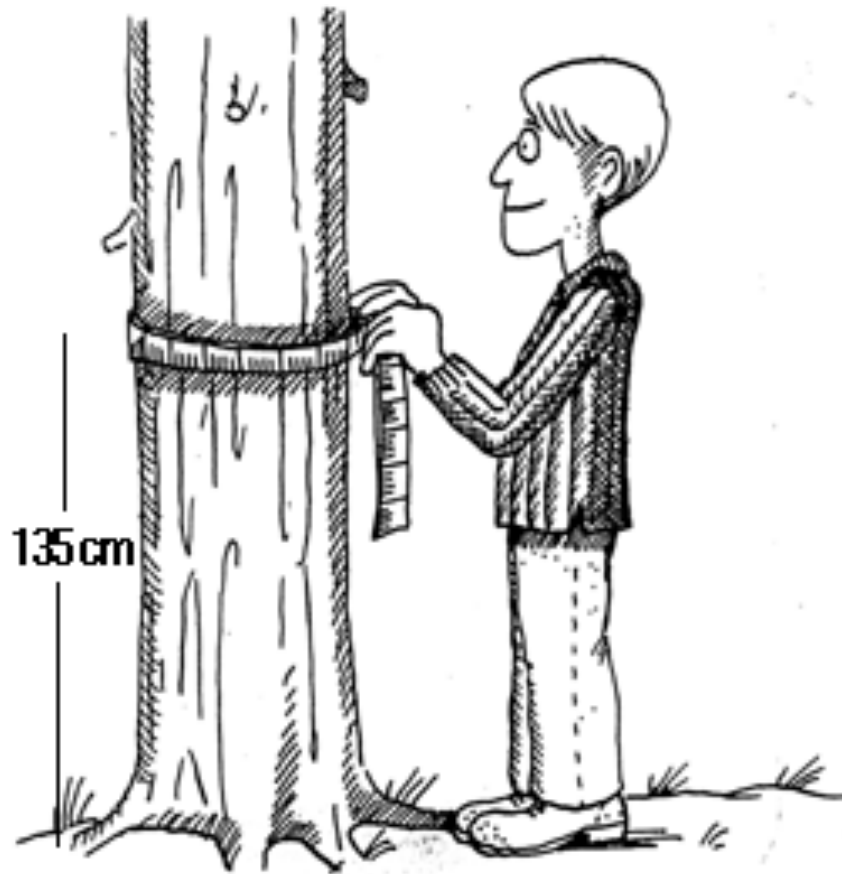
135cm off the ground



# Diameter at Breast Height (dbh)

After species & location, one of the most informative variables about a tree is dbh

135cm off the ground



🍌 for 🤔: Just whose breast height are we talking about?

**Question 0: What data did  
we collect and how?**



# Liriodendron Tulipifera i.e. Tulip Poplar

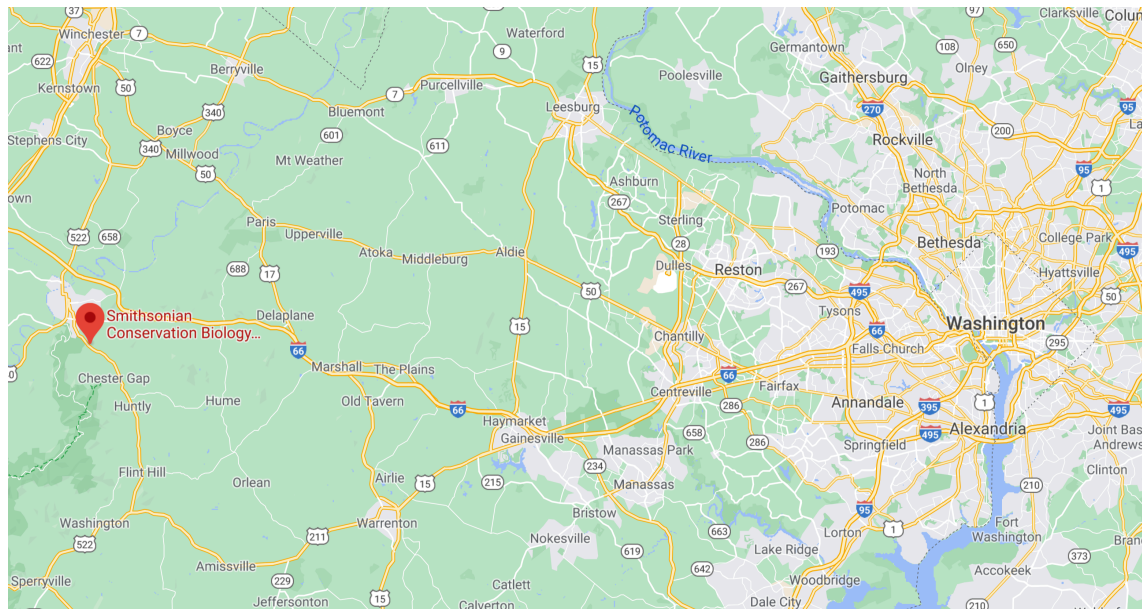


State tree of Indiana, Kentucky, & Tennessee.

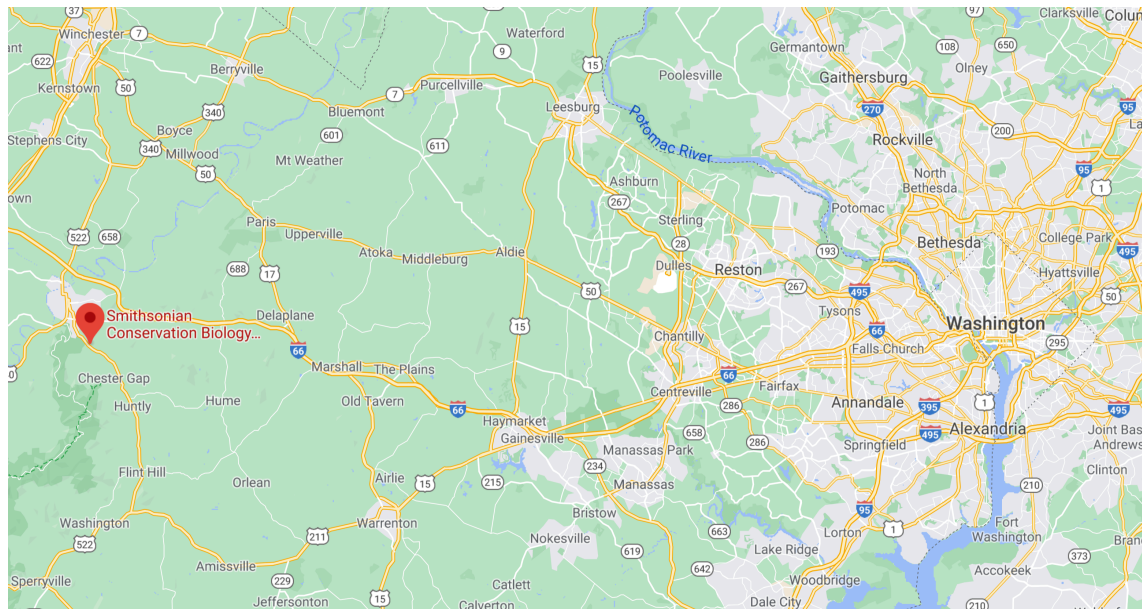


One particular tulip poplar

# One particular tulip poplar



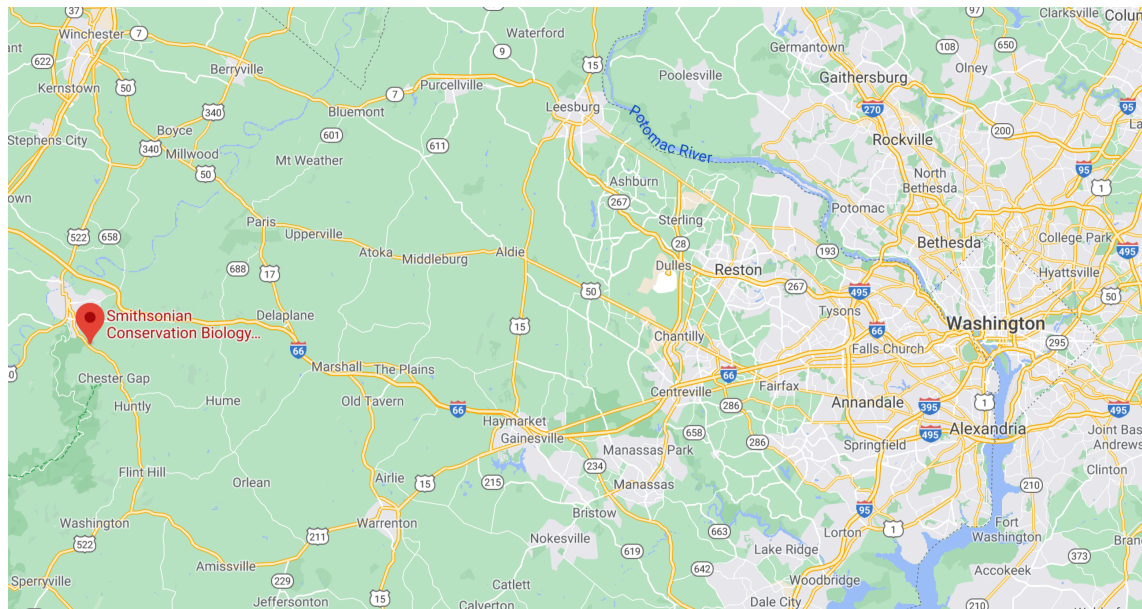
# One particular tulip poplar



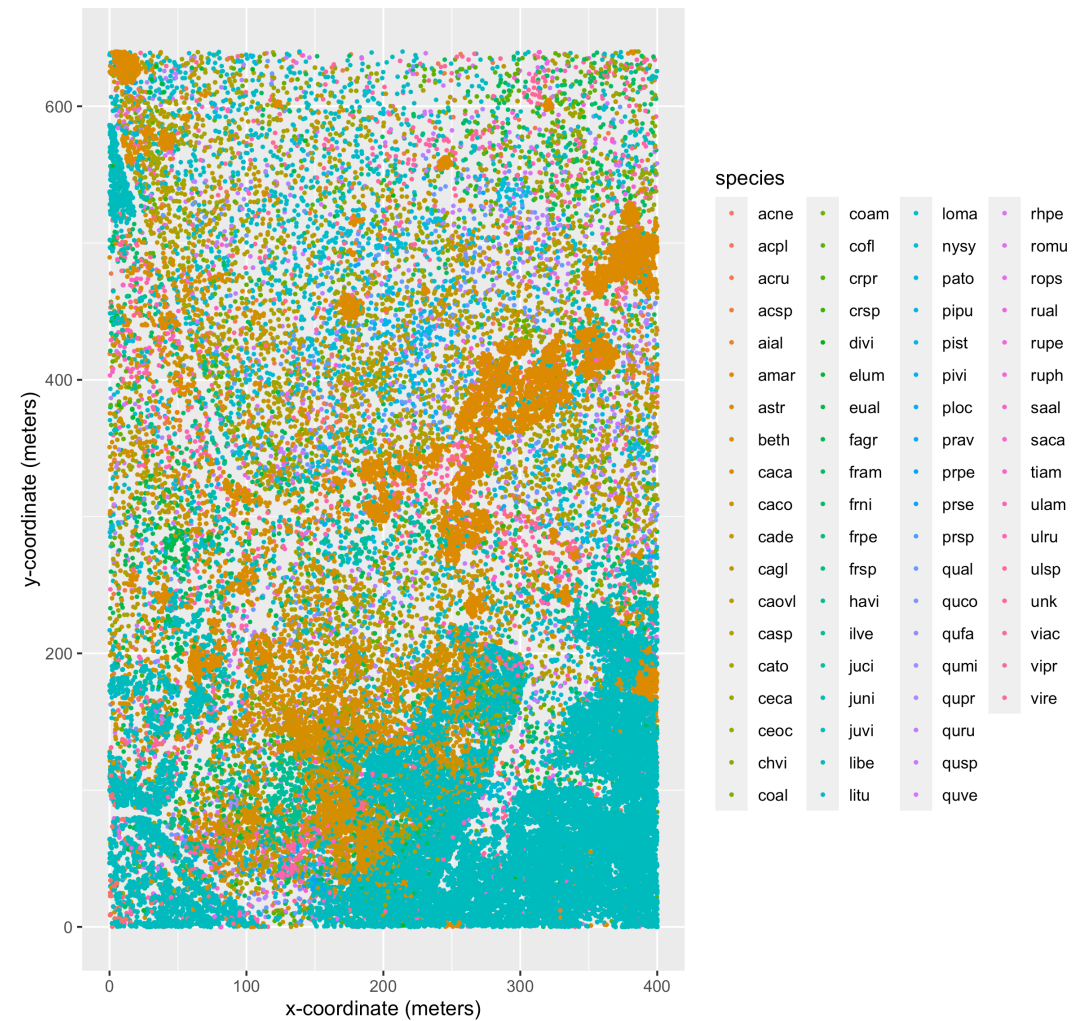
25.6 ha = 35.85 soccer fields



# One particular tulip poplar



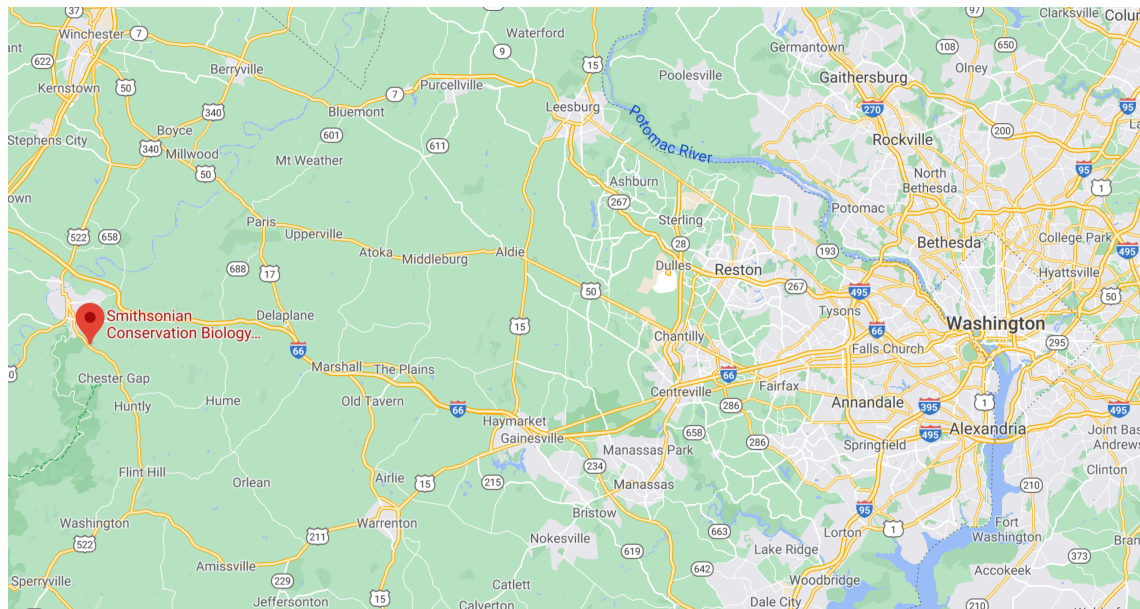
Census 2018: 72,555 cataloged trees



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# One particular tulip poplar



Census 2018: 72,555 cataloged trees



Tag 082422

25.6 ha = 35.85 soccer fields




# 1. Measure diameter w/ dendroband + calipers






# 2. Share Data on GitHub

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SCBI-ForestGEO / Dendrobands Unwatch 5 Star 0 Fork 0

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master Dendrobands / data / scbi.dendroAll\_2020.csv Go to file

 **rudeboybert** Replace text month coding with integer month coding for 2019 & 2020. F... Latest commit aa41236 on Jul 3 History

4 contributors

1280 lines (1280 sloc) 190 KB Raw Blame 

Search this file...

	tag	stemtag	survey.ID	year	month	day	biannual	intraannual	sp	quadrat	lx	ly	measure	codes	notes
1	10469	1	2020.01	2020	3	11	1	0	litu	109	9.7	1	NA	RE	window too large to measure
2	10587	1	2020.01	2020	3	11	1	0	litu	113	2.6	13	61.41	NA	NA
3	10609	1	2020.01	2020	3	11	1	0	cagl	111	19.5	2.9	81.03	NA	double-checked

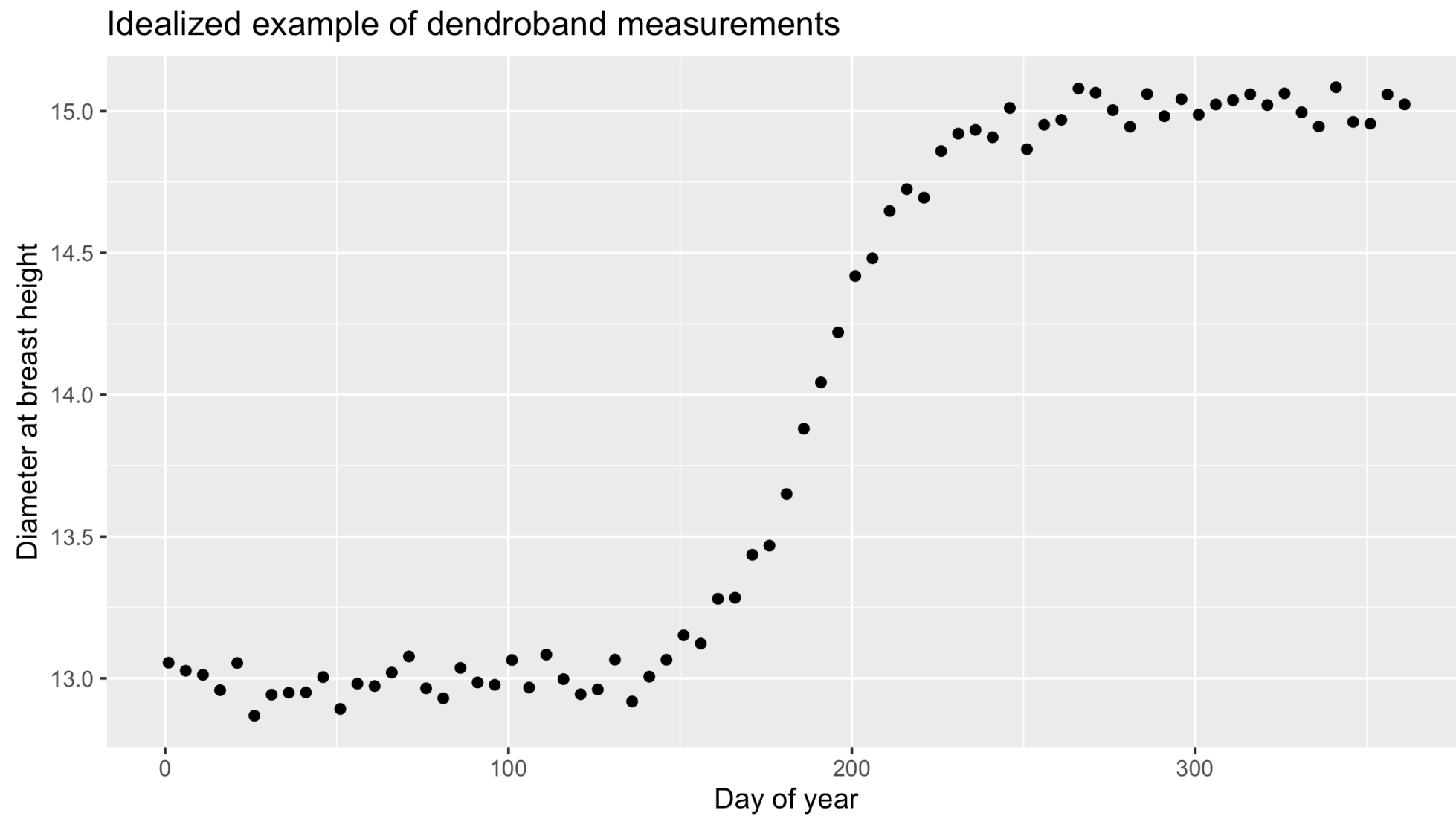


## 2. Share Data on GitHub

The screenshot shows the GitHub interface for the repository `SCBI-ForestGEO / Dendrobands`. The file `scbi.dendroAll_2020.csv` is selected, showing 1280 lines (1280 sloc) and 190 KB. The commit history shows a recent commit by `rudeboybert` on Jul 3. The file content is displayed as a table with columns: `tag`, `stemtag`, `survey.ID`, `year`, `month`, `day`, `biannual`, `intraannual`, `sp`, `quadrat`, `lx`, `ly`, `measure`, `codes`, and `notes`. The first four rows of data are visible, with the `tag`, `year`, `month`, `day`, and `measure` columns highlighted by red boxes.

	tag	stemtag	survey.ID	year	month	day	biannual	intraannual	sp	quadrat	lx	ly	measure	codes	notes
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### 3. Load data into statistical software



**Lesson 1: Numbers are  
numbers, but data has  
context.**

Question 1: How can we  
model within-year tree  
growth?



# Models

$$y = f(x) + \epsilon$$

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Models in general:

- $y$  = outcome you want to explain
- $x$  = input info
- $f$  = function connecting  $y$  &  $x$
- epsilon = error

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Model for dbh from dendrobands

- $y$  = dbh
- $x$  = day of year where Jan 1st = 1
- $f$  = function connecting  $y$  &  $x$
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# Models

$$y = f(x) + \epsilon$$

Models in general:

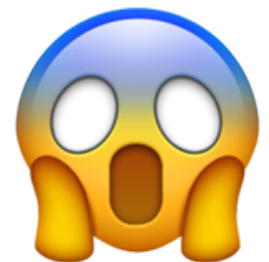
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Model for dbh from dendrobands

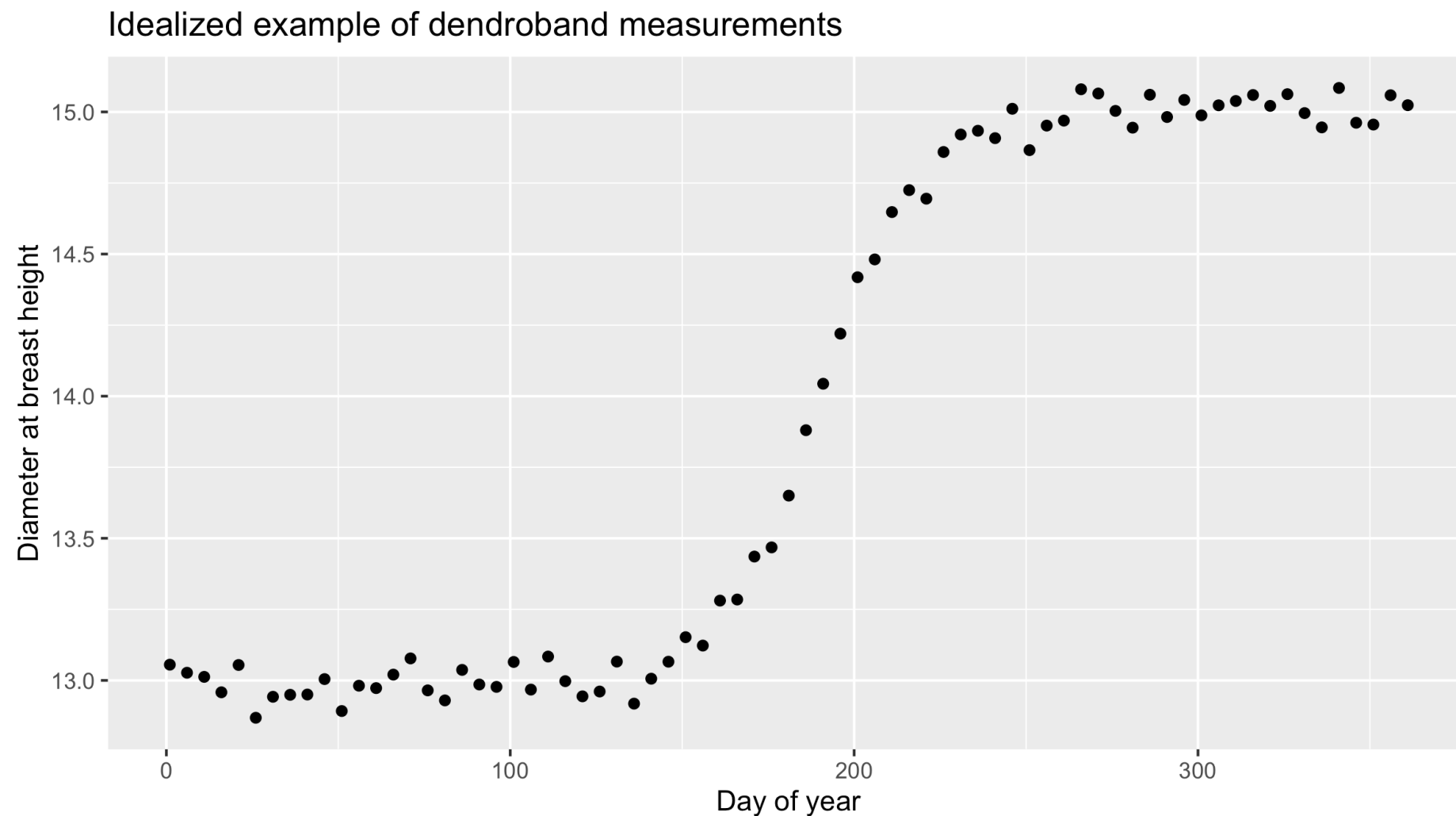
- $y$  = dbh
- $x$  = day of year where Jan 1st = 1
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- epsilon = measurement error, etc

$$dbh = \frac{L + (K - L)}{1 + 1/\theta \cdot \exp\left(-r(doy - doy_{ip})/\theta\right)} + \epsilon$$



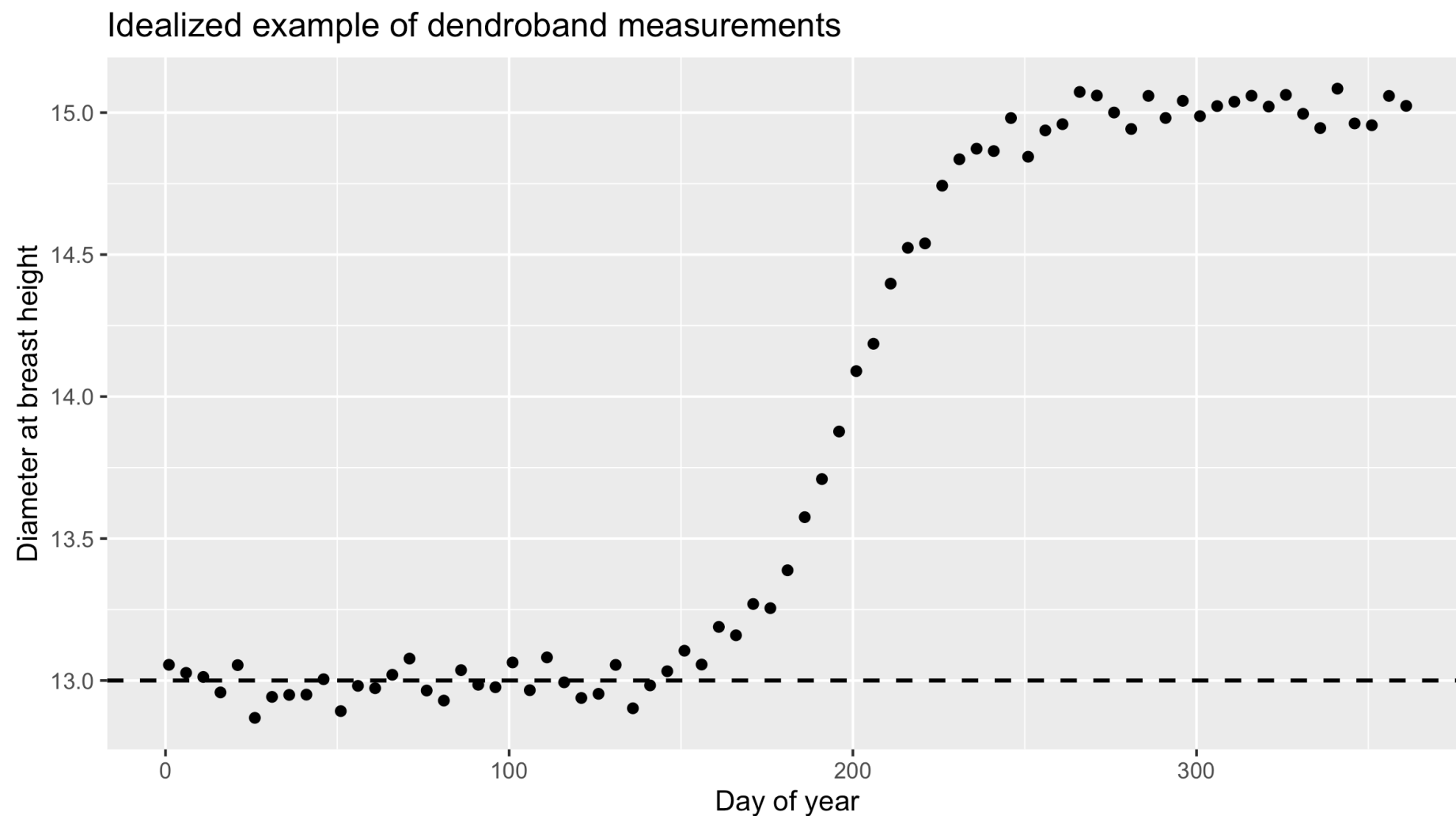
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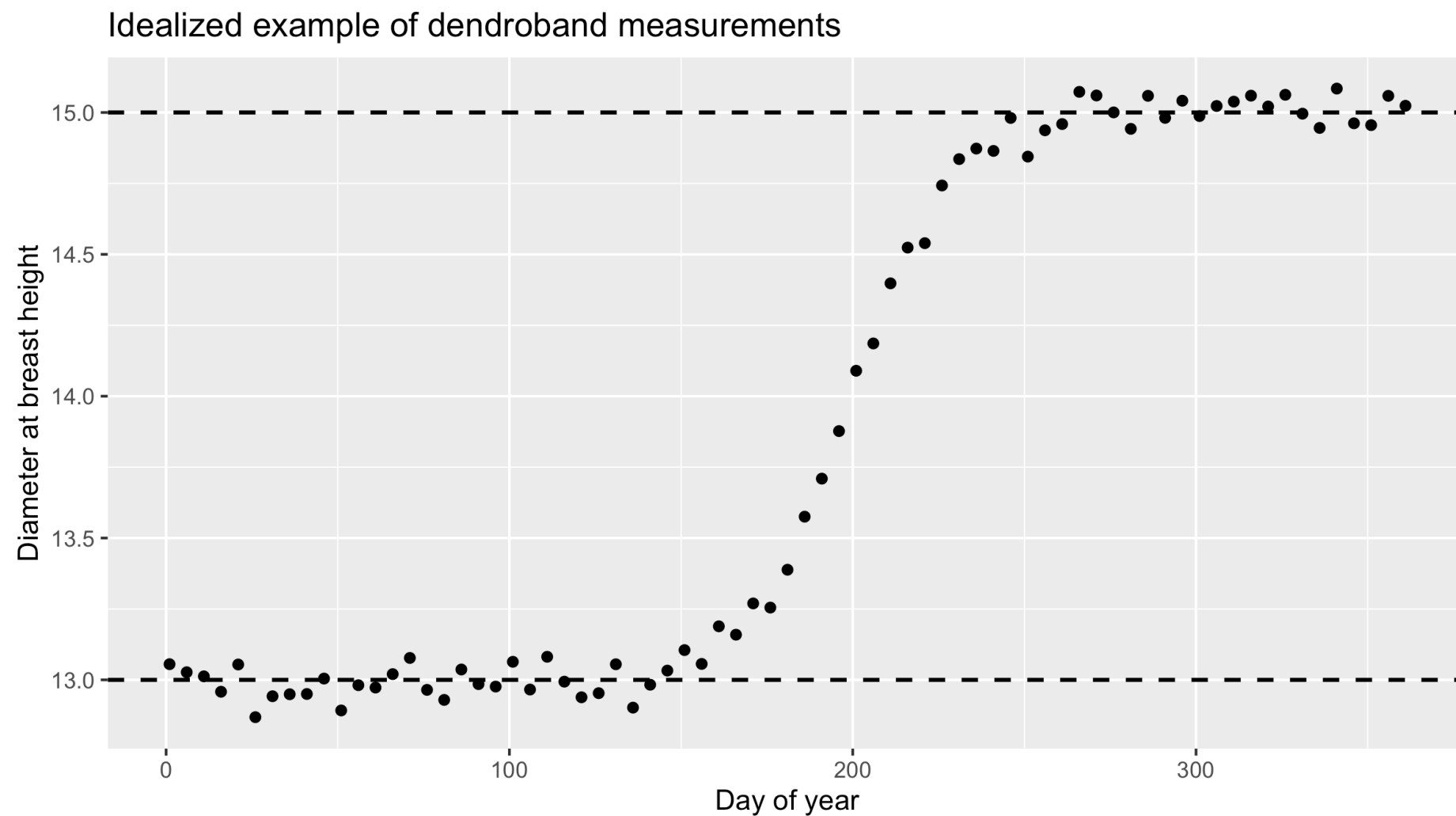
# Model for dbh

$$dbh = \frac{\boxed{L} + (K - \boxed{L})}{1 + 1/\theta \cdot \exp\left(-r(doy - doy_{ip})/\theta\right)^\theta}$$



# Model for dbh

$$dbh = \frac{L + \boxed{K} - L}{1 + 1/\theta \cdot \exp\left(-r(doy - doy_{ip})/\theta\right)^\theta}$$

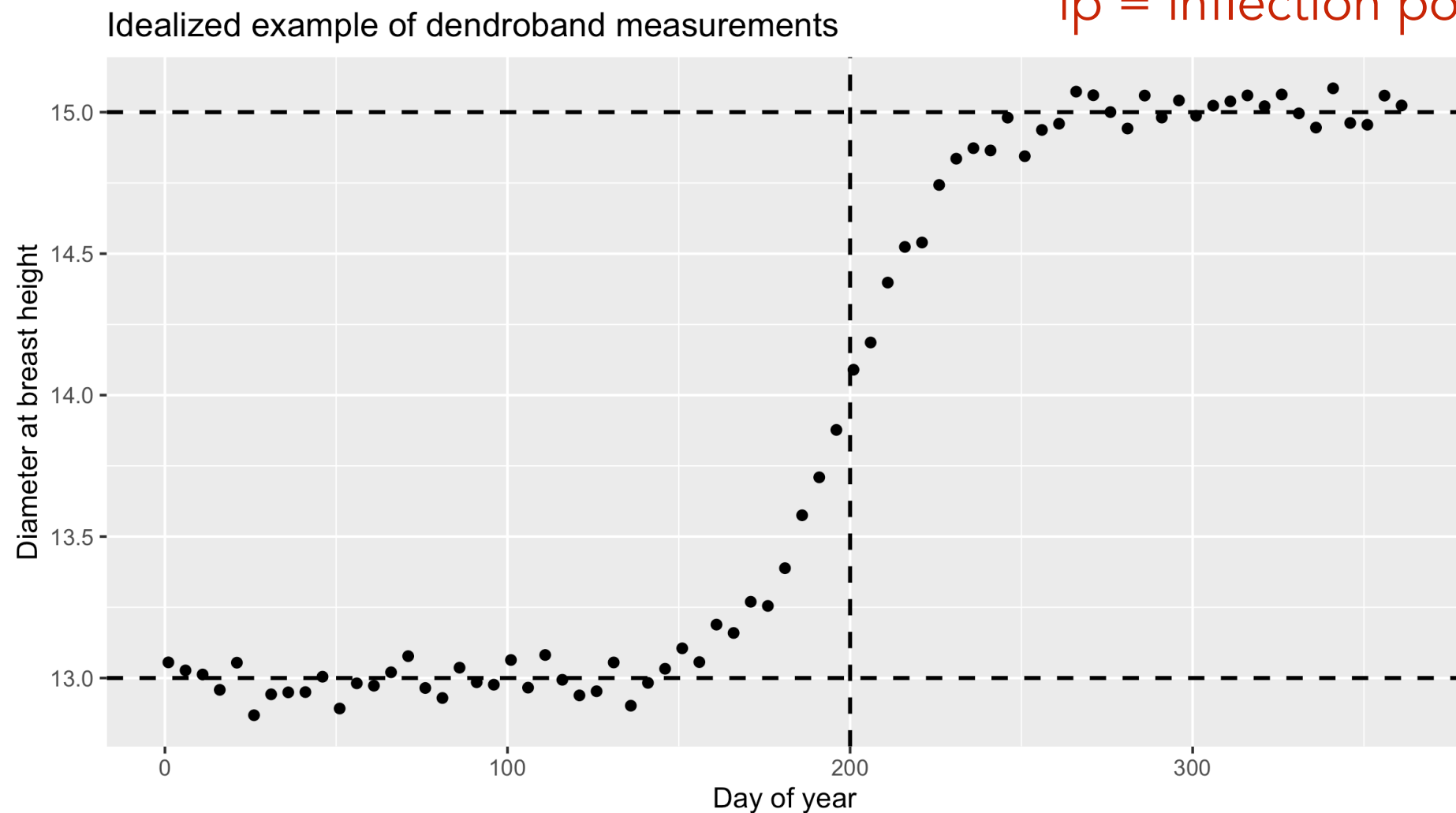




# Model for dbh

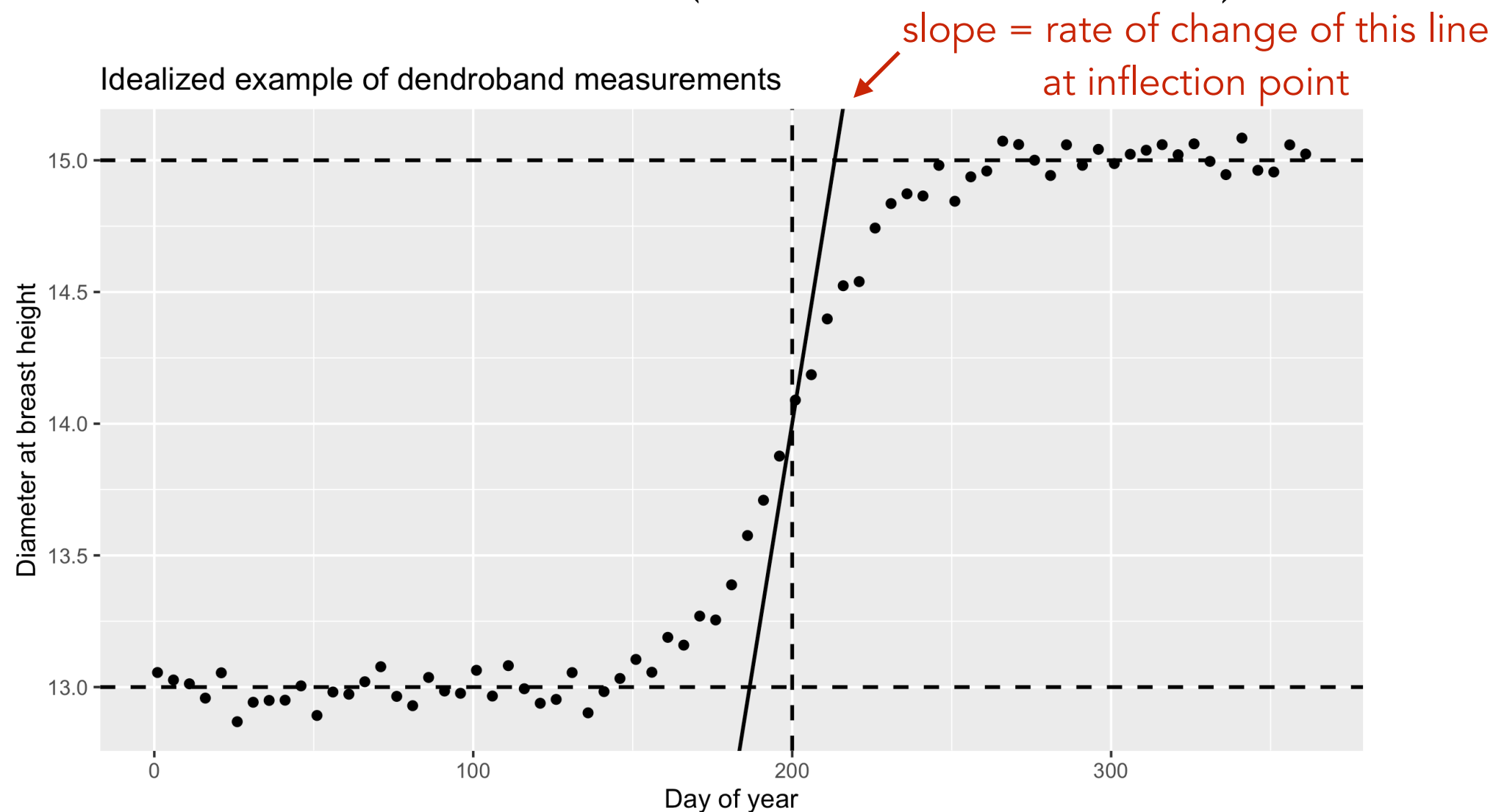
$$dbh = \frac{L + (K - L)}{1 + 1/\theta \cdot \exp\left(-r(doy - \boxed{doy_{ip}})/\theta\right)}^{\theta}$$

ip = inflection point



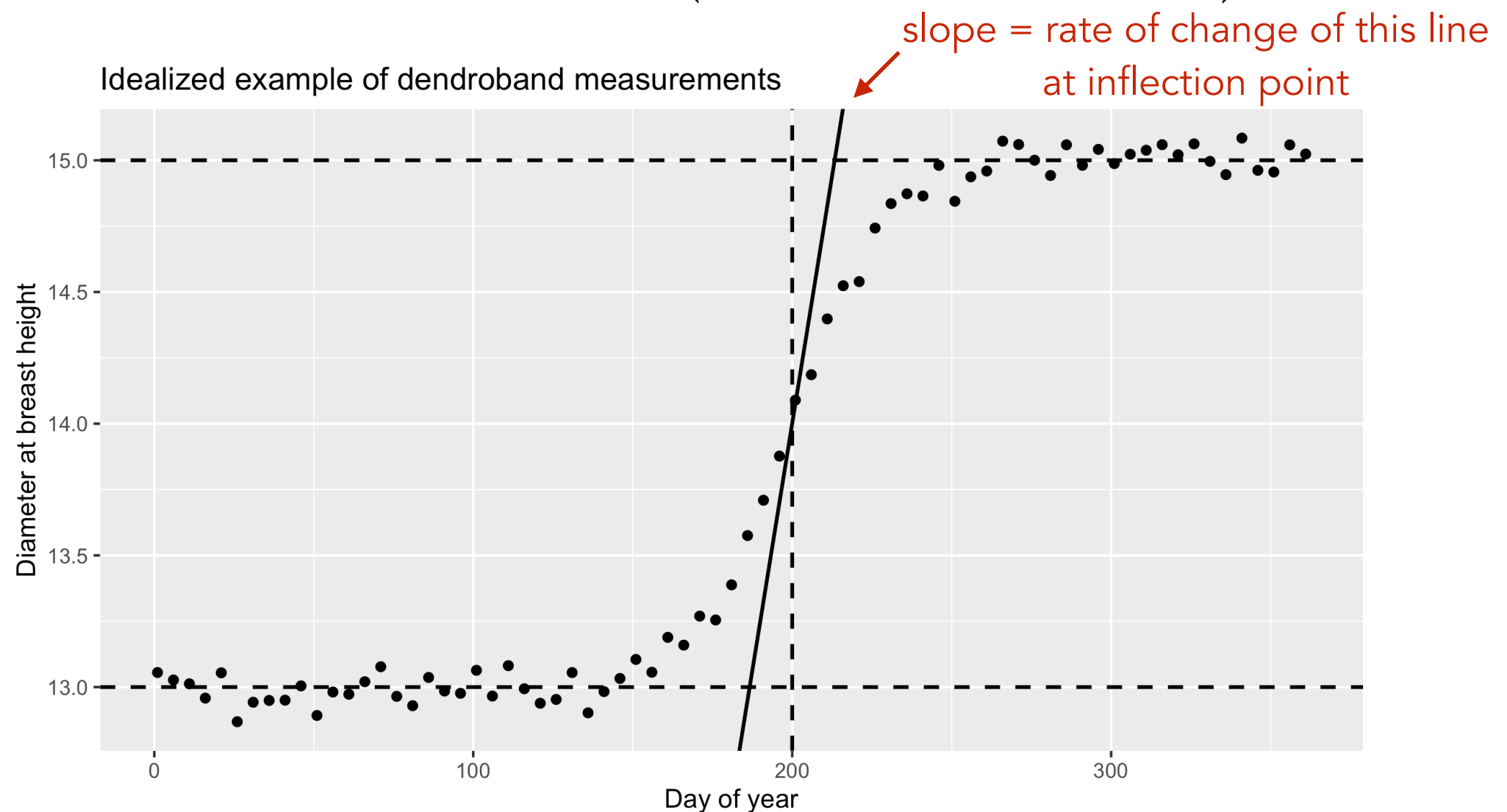
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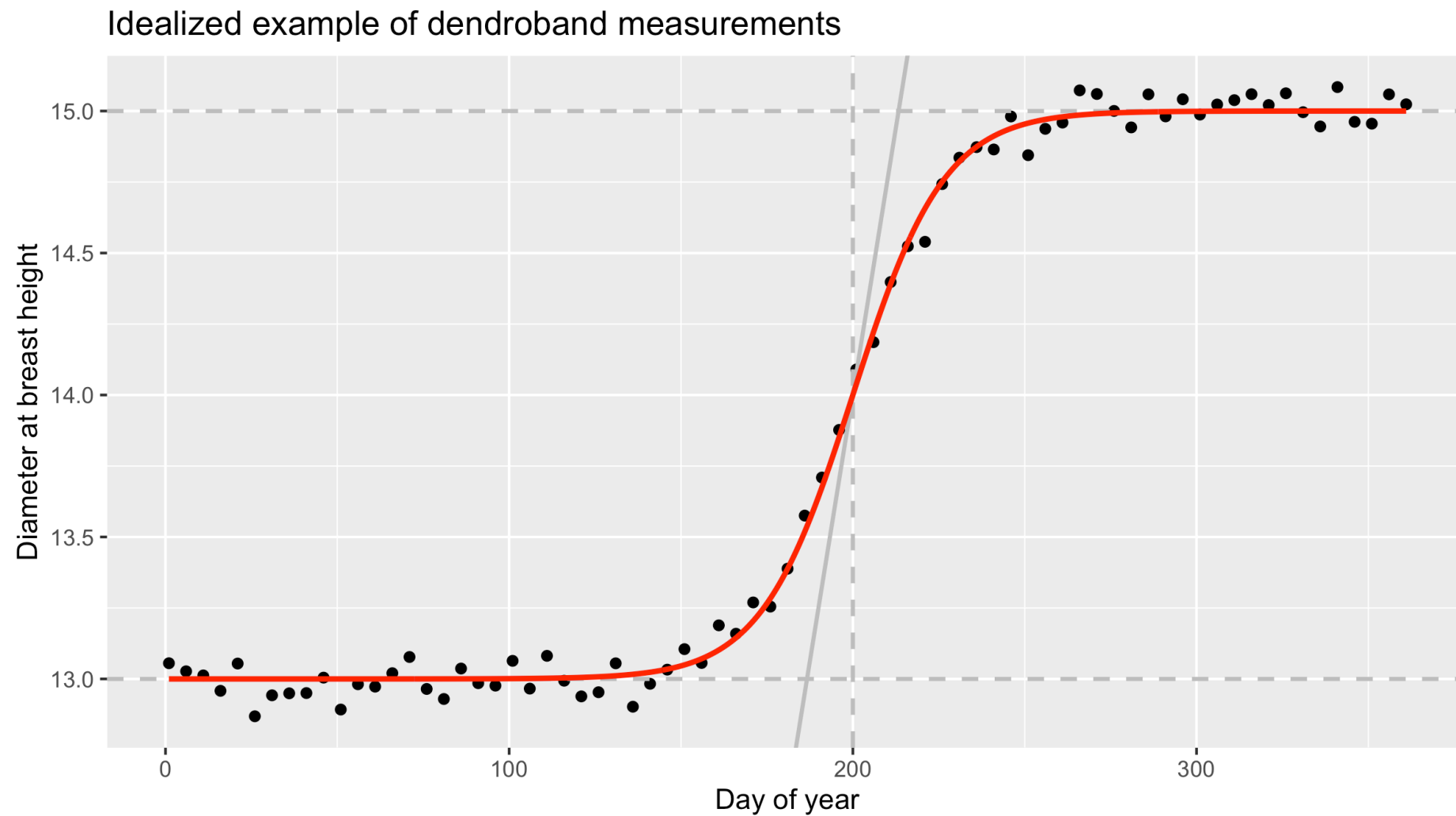
$$dbh = \frac{L + (K - L)}{1 + 1/\theta \cdot \exp\left(-\boxed{r}(doy - doy_{ip})/\theta\right)^\theta}$$



Ignoring  $\theta$ , let's put it all together...

# Model for dbh

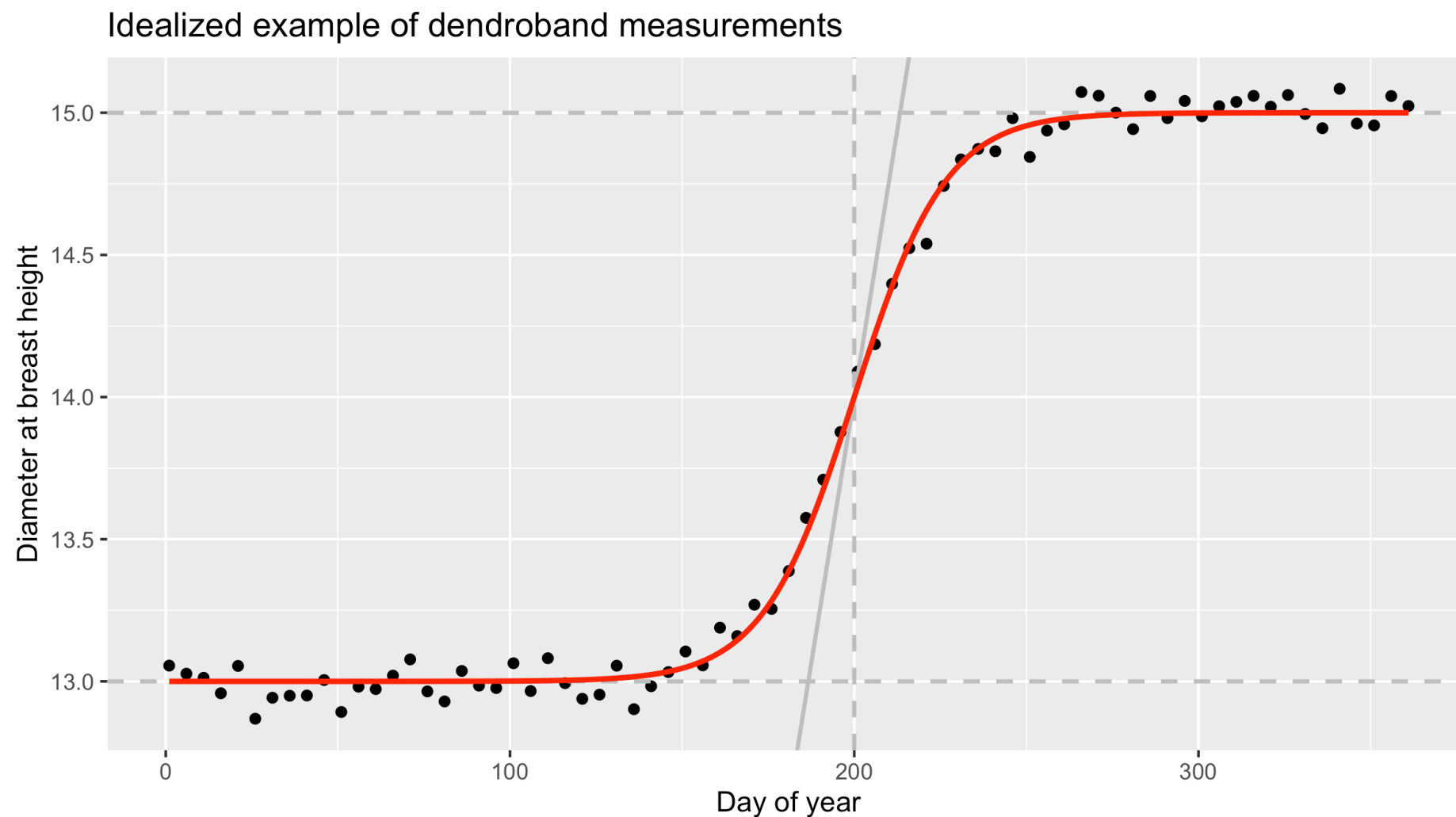
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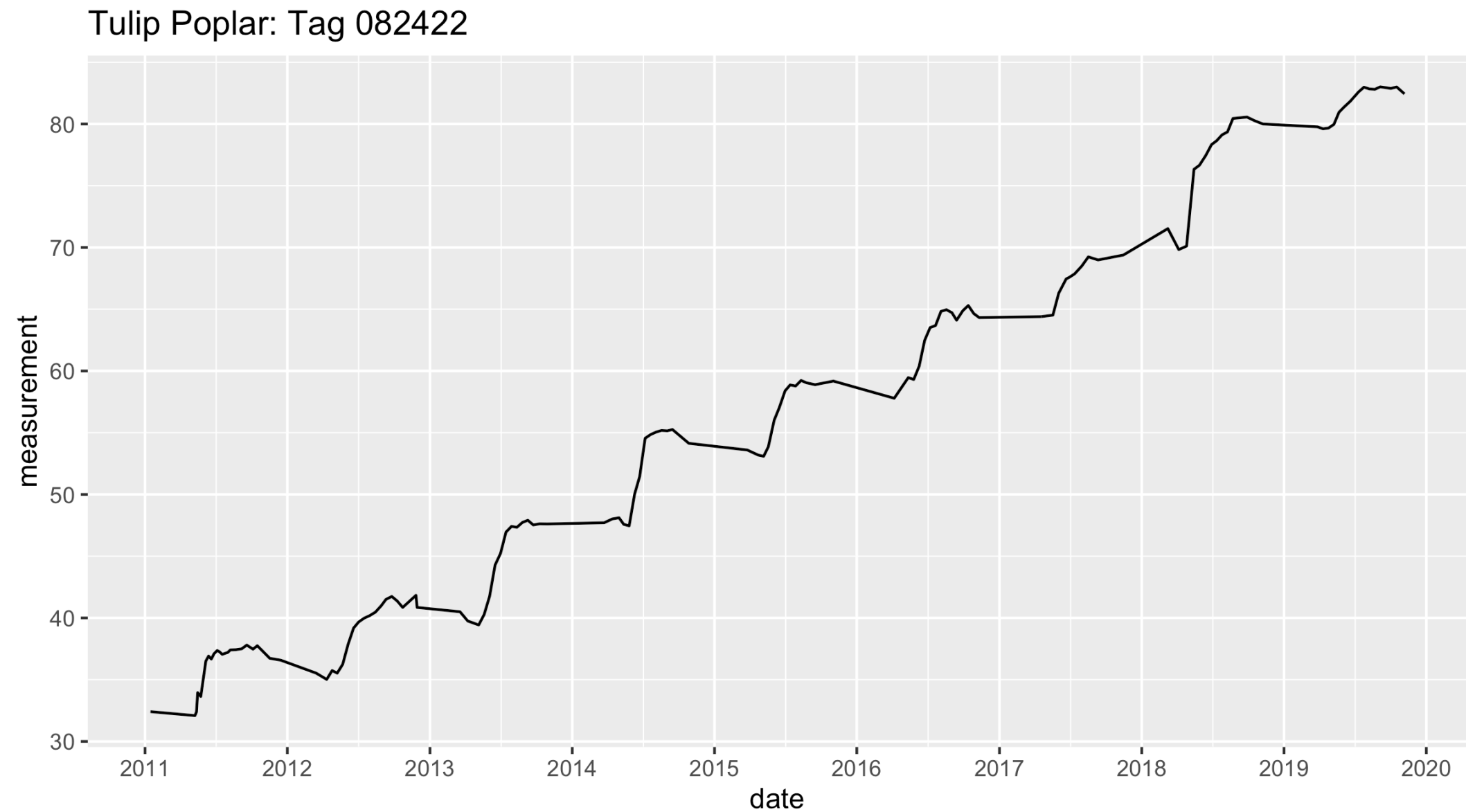


But remember, you need a model that works for ALL 🌲🌳🌴

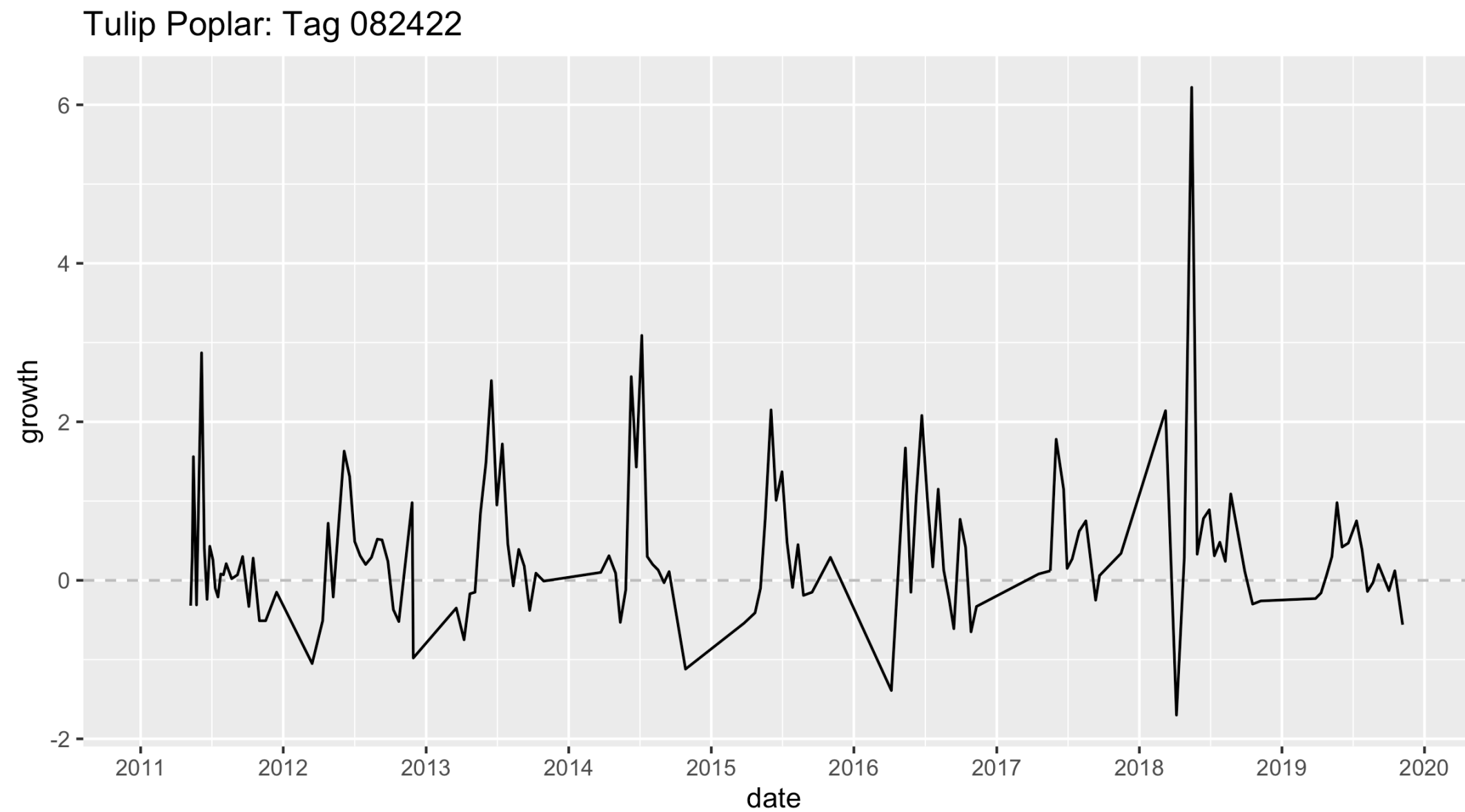
Lesson 2: Statistics is not  
math, rather statistics uses  
math

**Question 2: How can we  
model the effect of climate  
change on growth?**

# Observed Dendroband Measurements



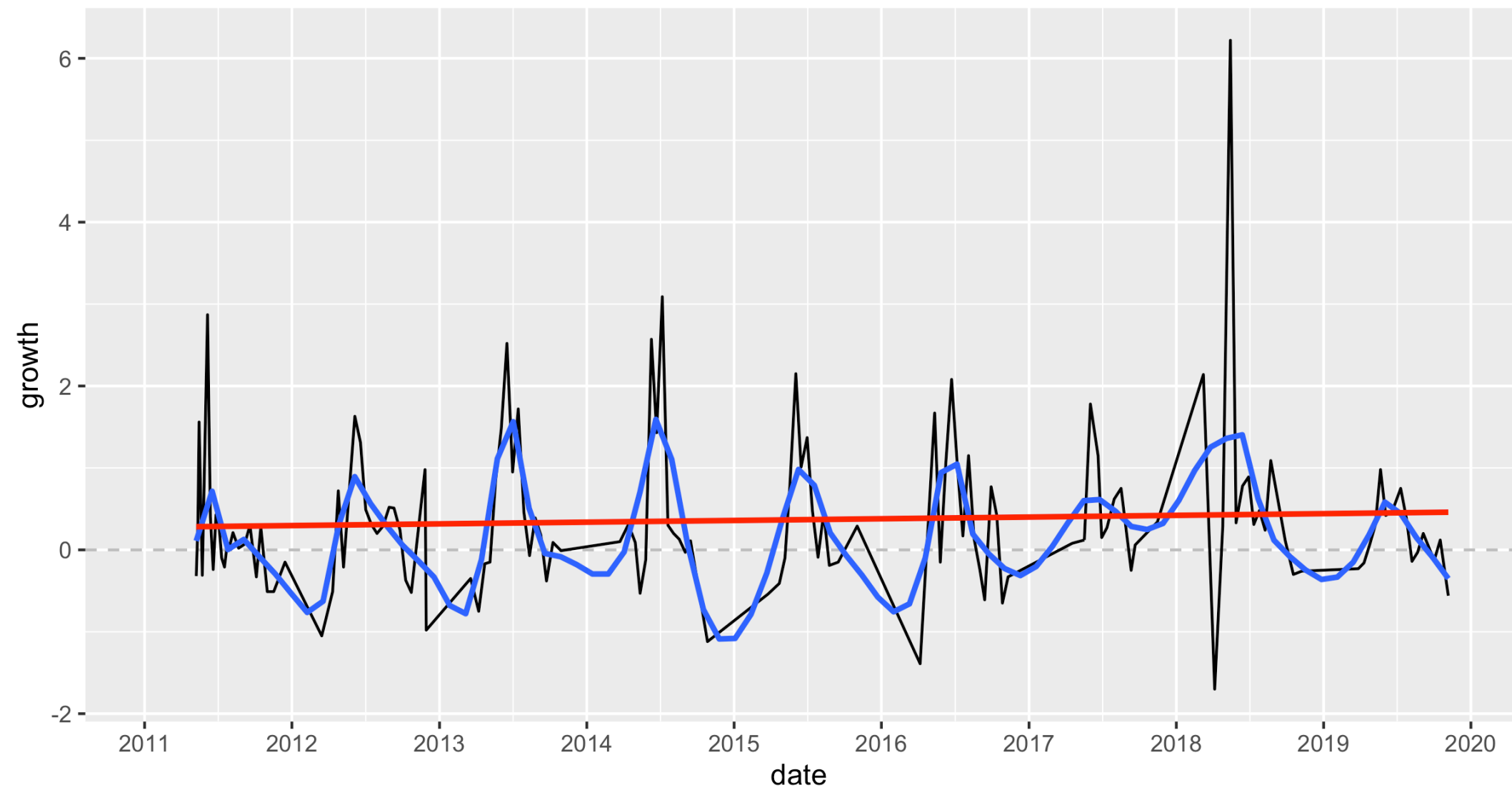
# Growth = difference in measurements



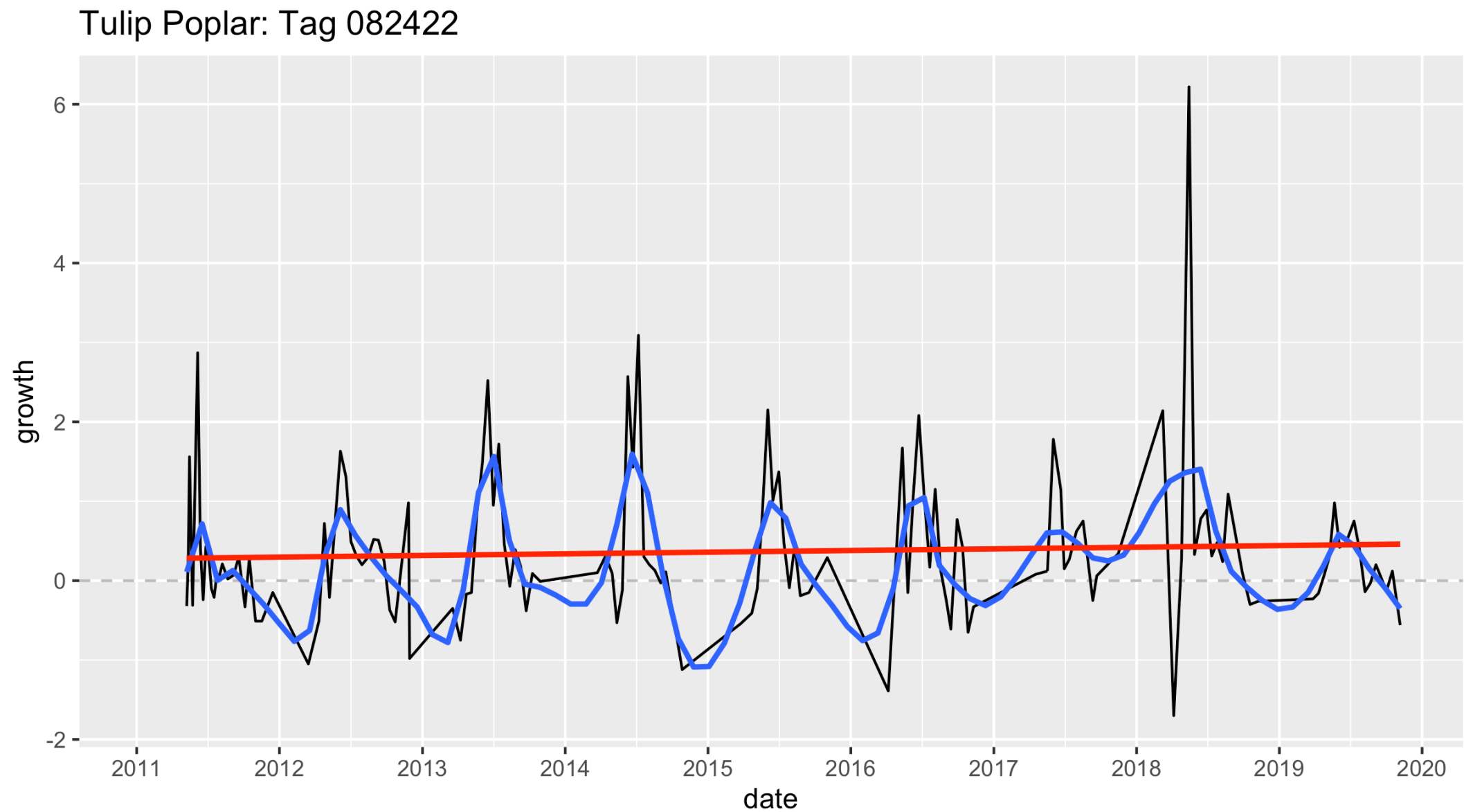


# Patterns

Tulip Poplar: Tag 082422

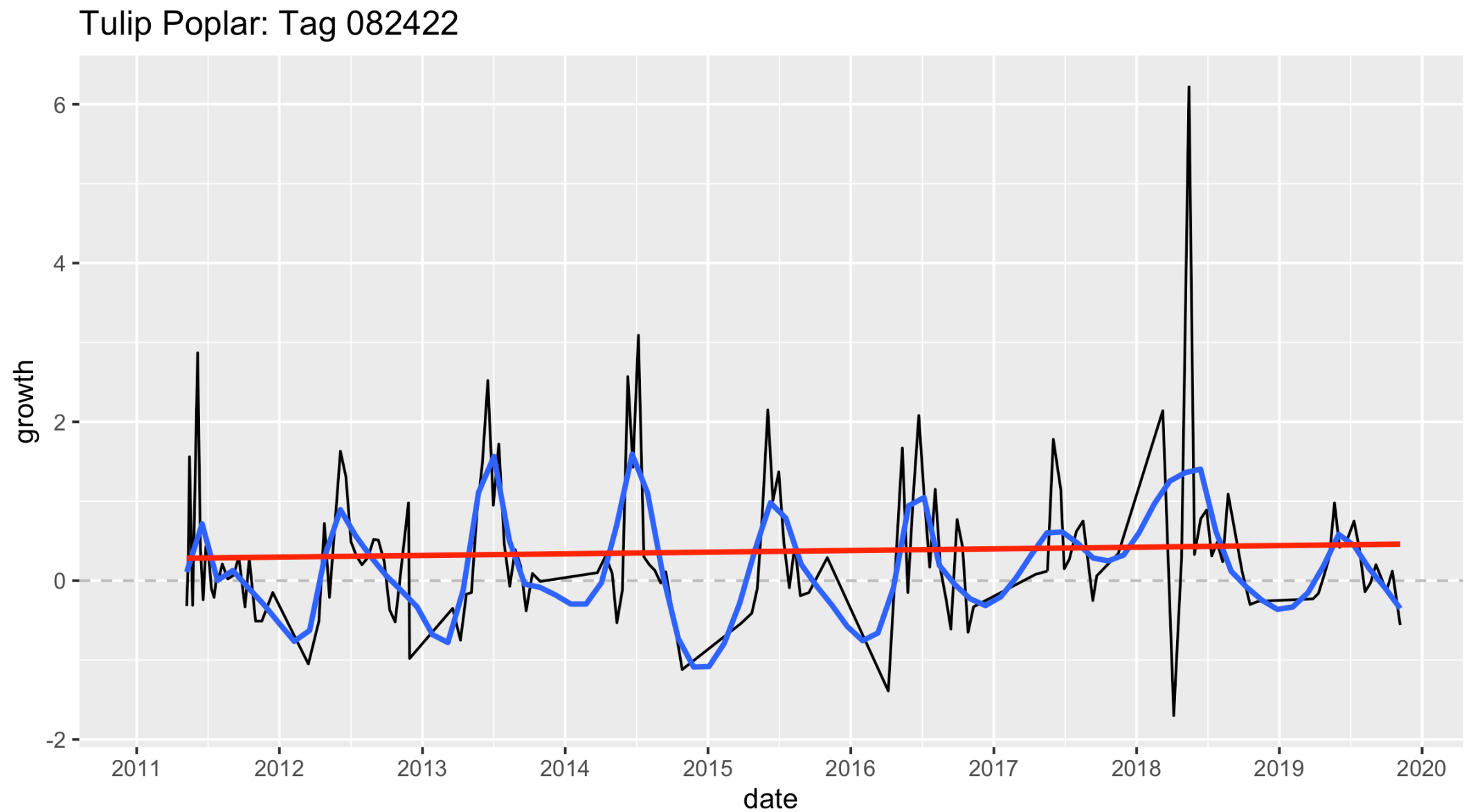


# Patterns



**Seasonal trend that repeats every year**

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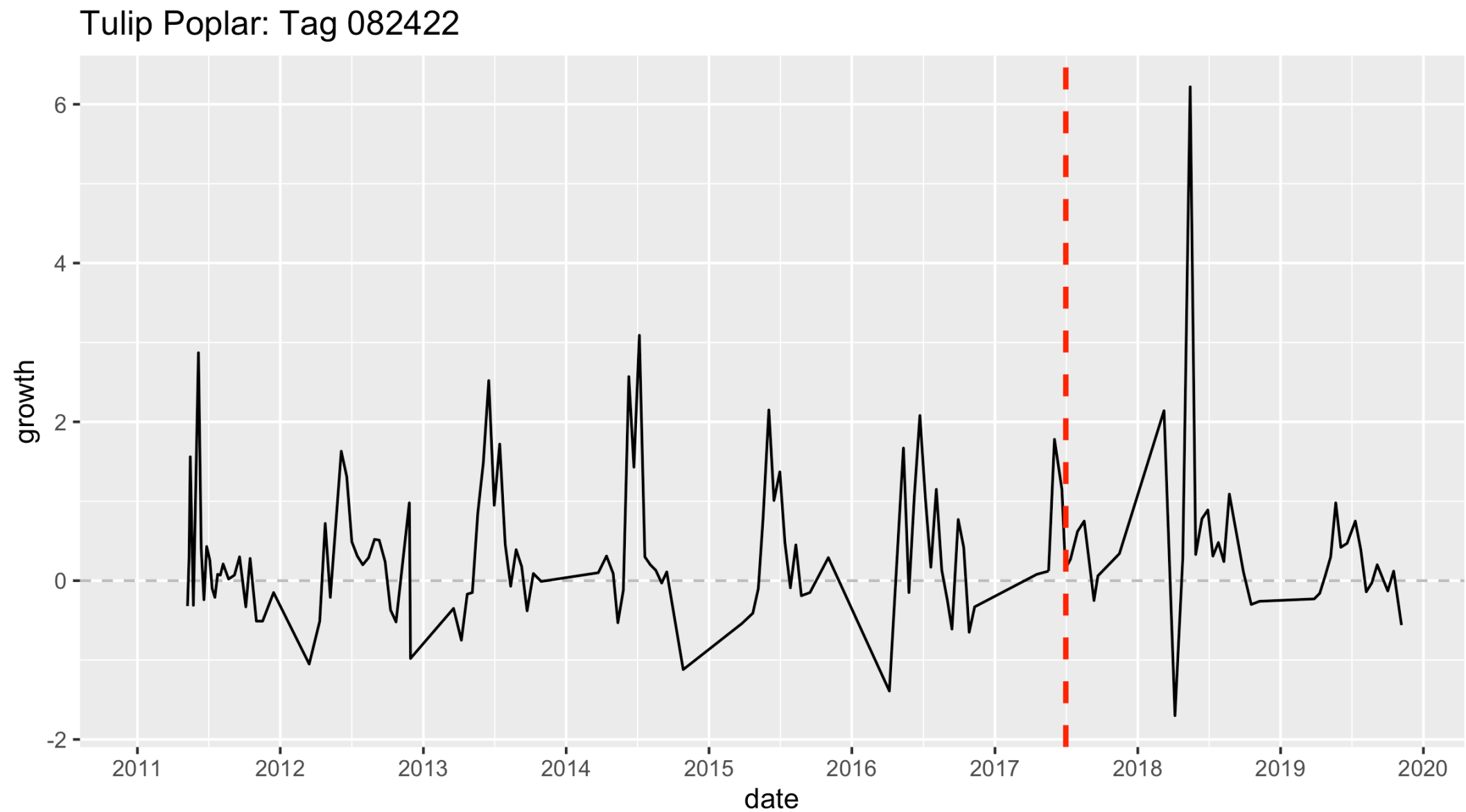


**Seasonal trend that repeats every year**

**Overall (slightly increasing) trend**



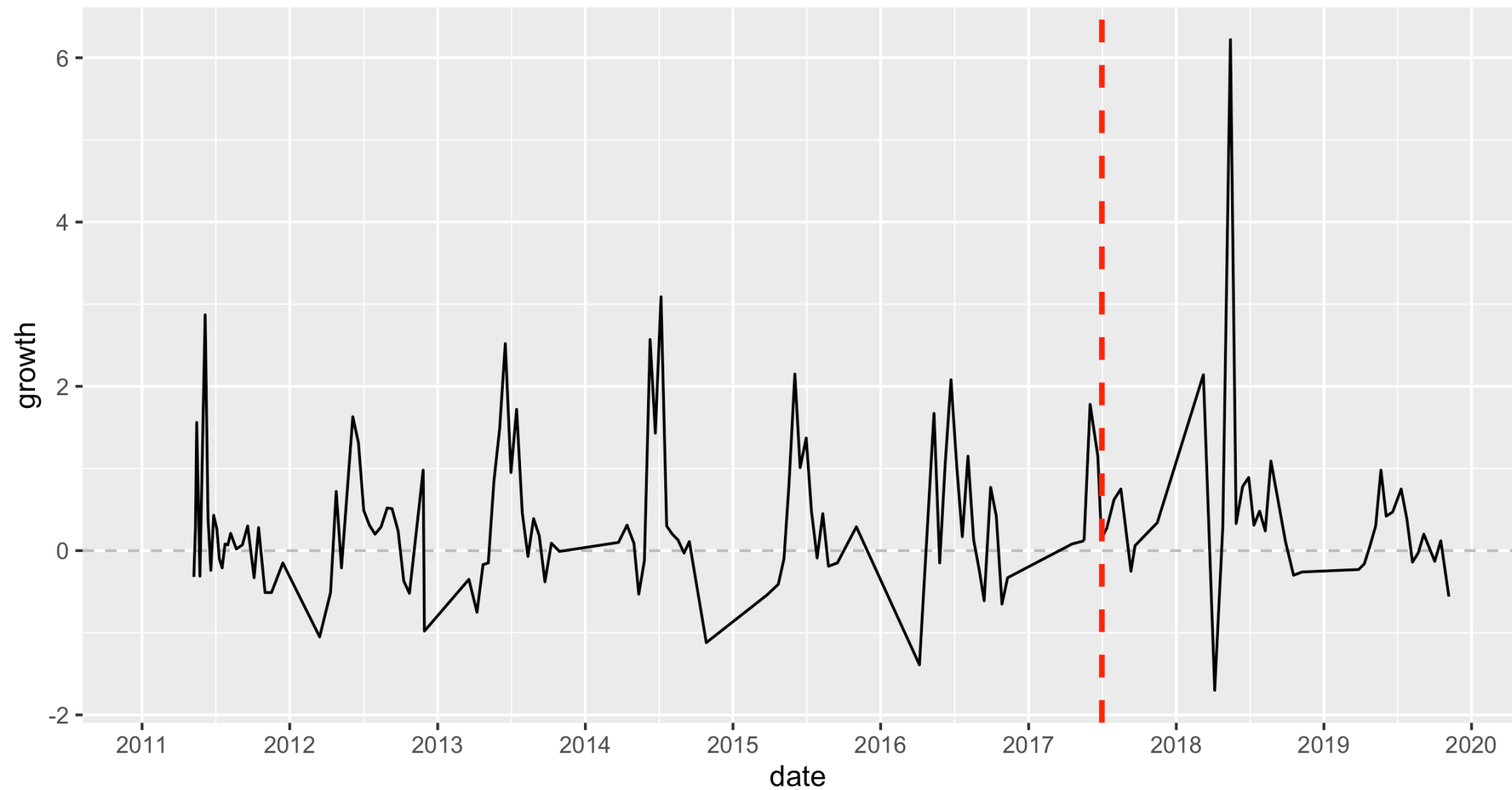
# Effect of Climate Change



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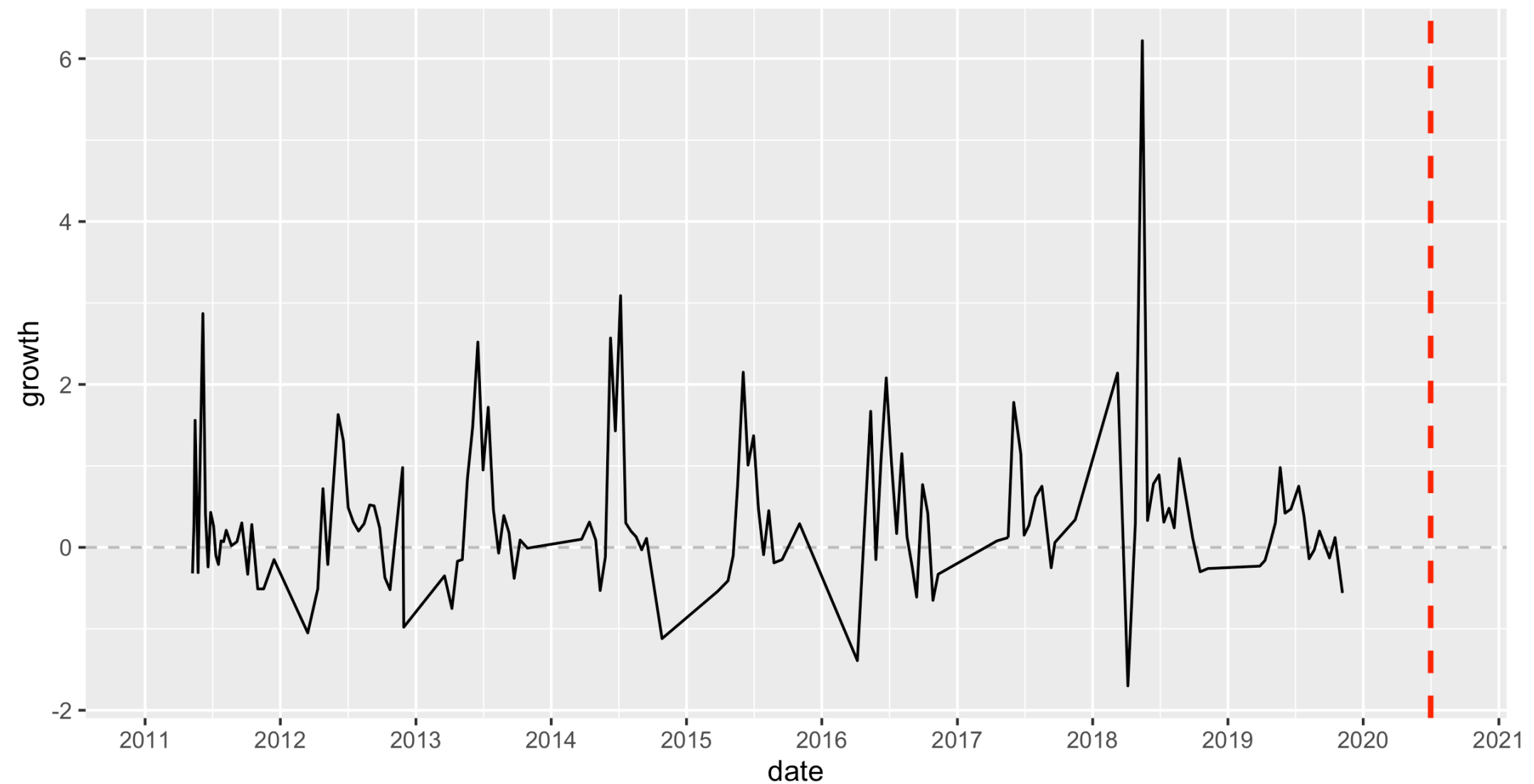
July 2017 was very hot 🥵



# Effect of Climate Change

July 2020 was even hotter 🔥😓🔥

Tulip Poplar: Tag 082422

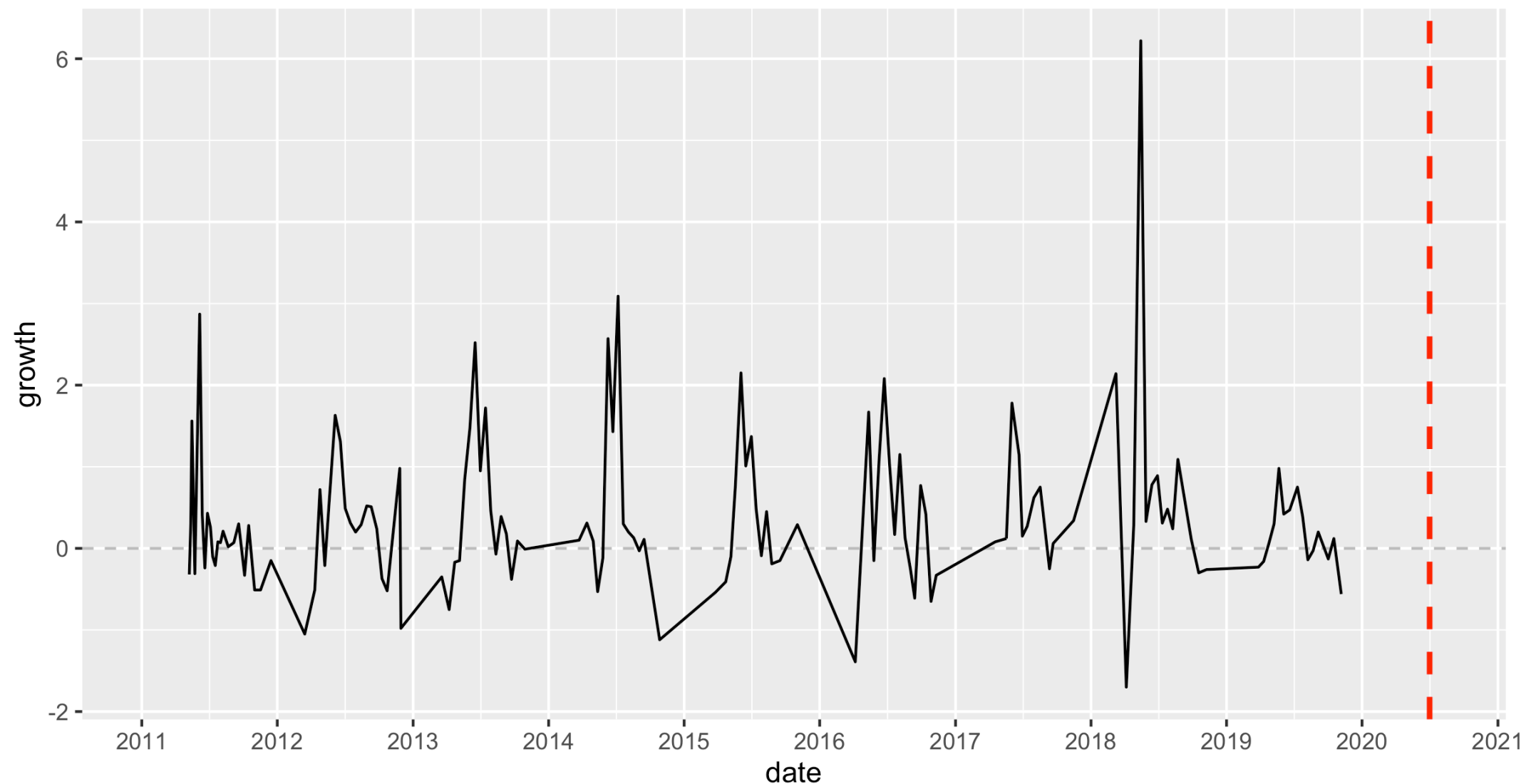




# Effect of Climate Change

July 2020 was even hotter 🔥😓🔥

Tulip Poplar: Tag 082422



What other variables should we account for?

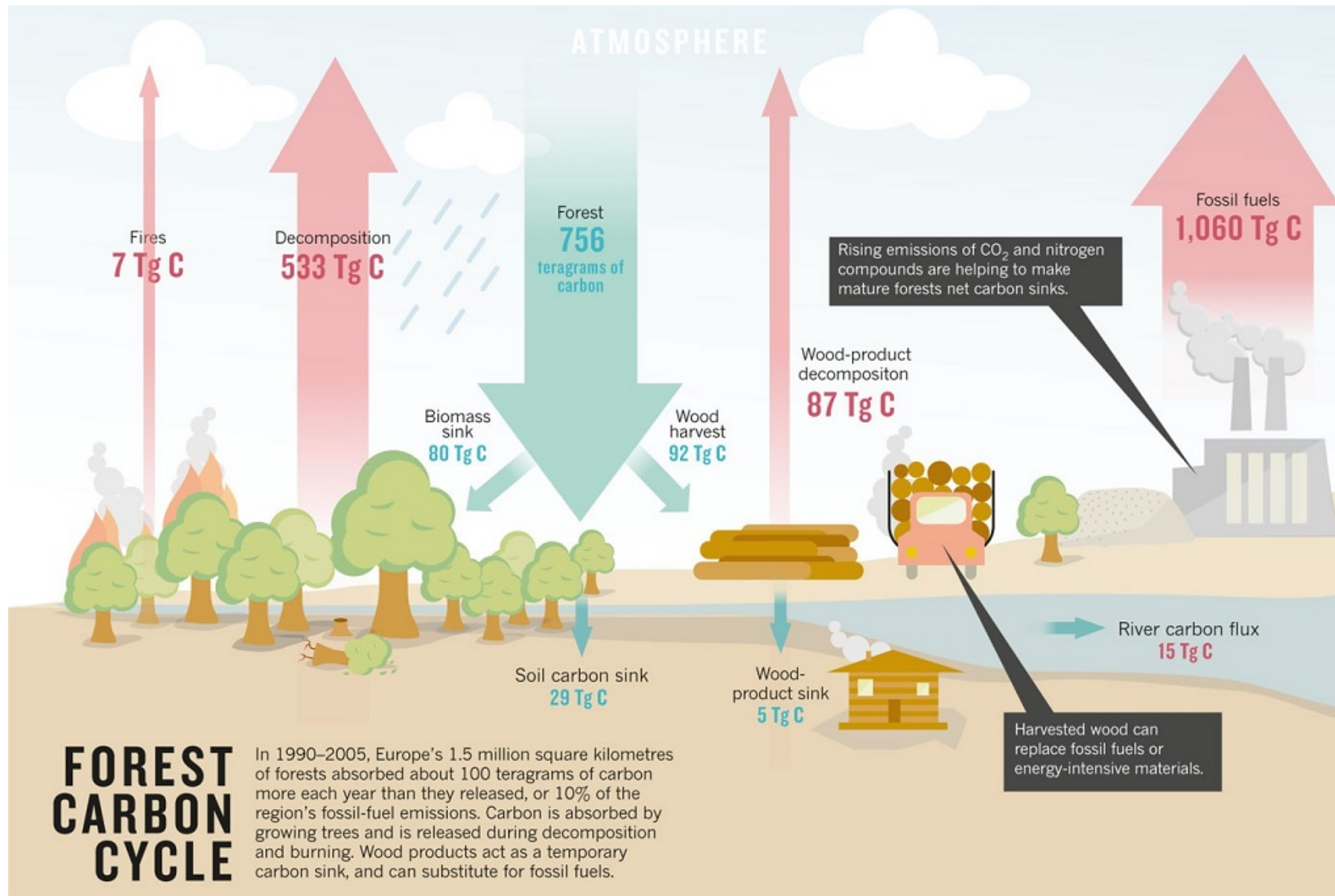
Drought? Humidity? Earlier springs?

Smoke from CA, WA, OR forest fires? etc...

**Lesson 3: "All models are  
wrong, but some are useful"**  
**George Box**

**Where is this headed?**

# Forests as Carbon Sinks





From yesterday's presidential "debate"

# From yesterday's presidential "debate"

On the topic of climate change...

## Is the U.S. Really Planting a Billion Trees, as Trump Said?

*Or maybe a trillion? Either way, it won't do much.*

By **Alissa Walker** | [@awalkerinLA](#) | Sep 30, 2020, 12:20am EDT

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Proof that Donald Trump has in fact planted one tree, with French president Emmanuel Macron in 2018. (It died.) | AFP via Getty Images

### MOST READ



Is the U.S. Really Planting a Billion Trees, as Trump Said?





# To plant or not to plant?



Regrowing trees soak up carbon in Brazil's Atlantic Forest northeast of Rio de Janeiro. ROBIN CHAZDON

## Plant trees or let forests regrow? New studies probe two ways to fight climate change

By **Gabriel Popkin** | Sep. 23, 2020 , 12:25 PM

# Model for Natural Regrowth

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Susan C. Cook-Patton , Sara M. Leavitt, [...] Bronson W. Griscom

*Nature* **585**, 545–550(2020) | [Cite this article](#)

**4647** Accesses | **564** Altmetric | [Metrics](#)

### Abstract

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To constrain global warming, we must strongly curtail greenhouse gas emissions and capture excess atmospheric carbon dioxide<sup>1,2</sup>. Regrowing natural forests is a prominent strategy for capturing additional carbon<sup>3</sup>, but accurate assessments of its potential are limited by uncertainty and variability in carbon accumulation rates<sup>2,3</sup>. To assess why and



# Model for Natural Regrowth

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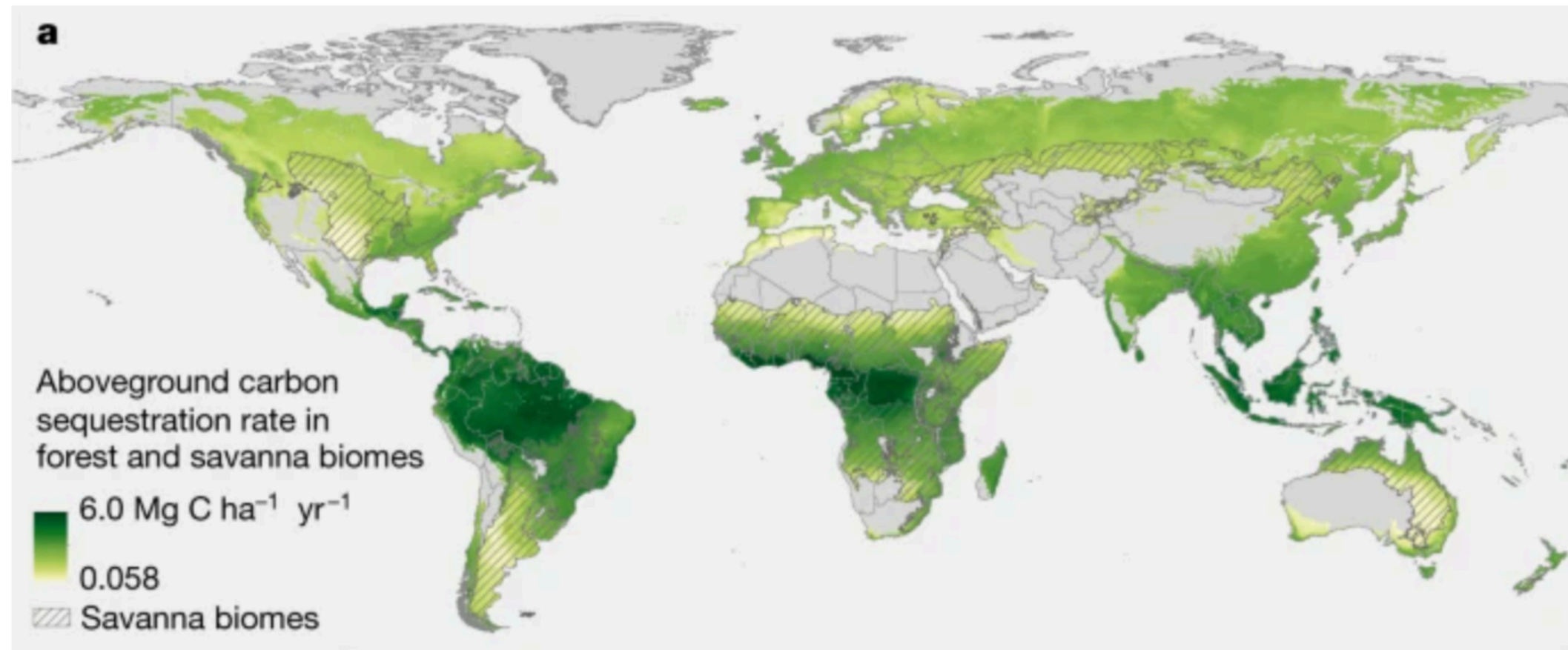
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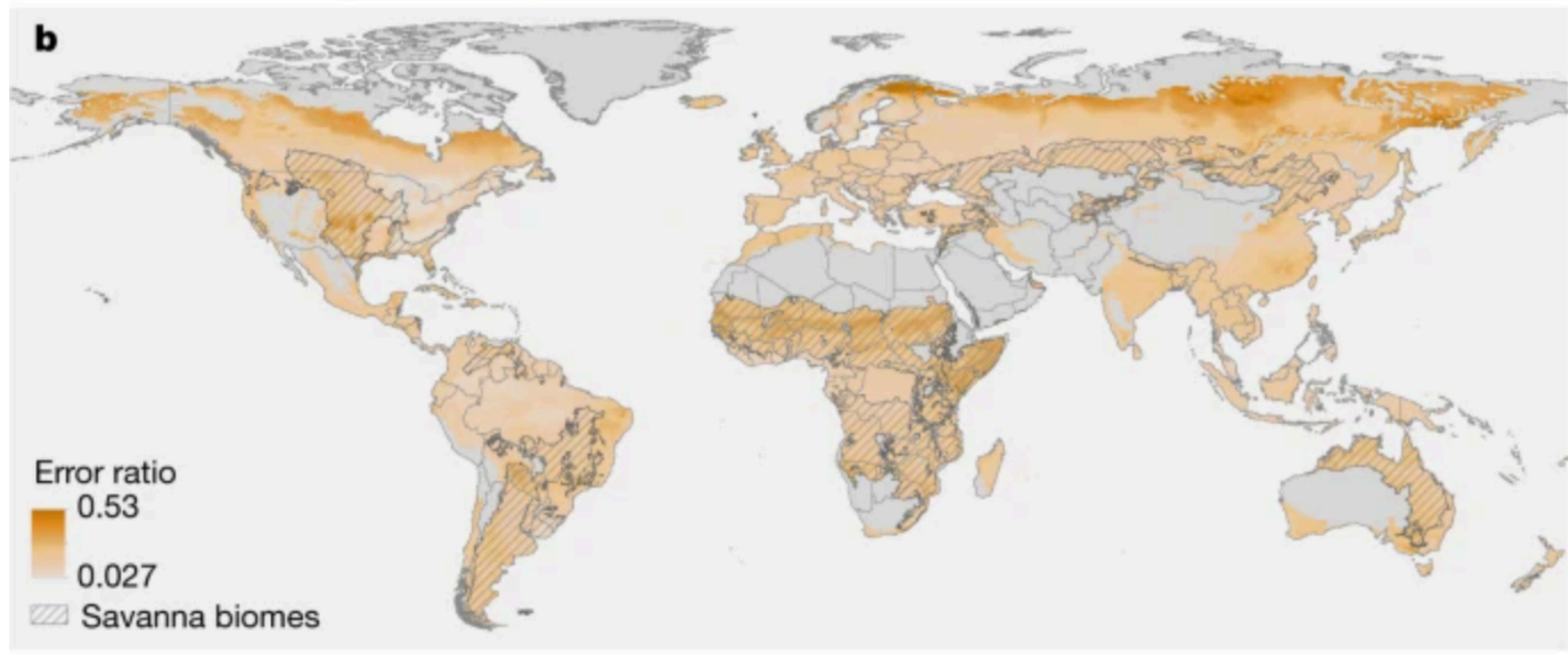
To constrain global warming, we must strongly curtail greenhouse gas emissions and capture excess atmospheric carbon dioxide<sup>1,2</sup>. Regrowing natural forests is a prominent strategy for capturing additional carbon<sup>3</sup>, but accurate assessments of its potential are limited by uncertainty and variability in carbon accumulation rates<sup>2,3</sup>. To assess why and



# Predicted/forecasted carbon accumulation



# All predictions/forecasts have errors too...



**Thanks!**

**Slides on Twitter  
@rudeboybert**